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**Application of Modified Gain Extended Kalman Filter for Underwater Passive
Target Tracking Using Angles Only Measurements**

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Abstract

Underwater, Passive Target tracking, for a moving observer, observation will be a critical task. Modified Gain Extended Kalman Filter (MGEKF) developed by Song and Speyer [3] was proven to be suitable algorithm for angles only passive target tracking applications in air. In this paper, this improved MGEKF algorithm is explored for underwater applications with some modifications. In underwater, the noise in the measurements is very high, turning rate of the platforms is low and speed of the platforms is also low when compared with the missiles in air. These characteristics of the platform are studied in detail and the algorithm is modified suitably for tracking applications in underwater. Monte-Carlo simulated results for one typical scenario is presented for the purpose of explanation. From the results it is observed that this algorithm is suitable for moving observer in underwater passive target tracking using angles only measurements.

Keywords: Kalman filter.

Introduction

In the ocean environment, an observer monitors noisy sonar bearings and elevations from a radiating target. These measurements are extracted by an observer moving in a straight line and the observer processes these measurements to find out target motion parameters-Viz., range, course, bearing, elevation and speed of the target. Here the measurements are nonlinear; making the whole process nonlinear. However, the modified gain extended kalman filter (MGEKF) developed by Song and Speyer [3], was the successful contribution for angles only passive target tracking applications in air. This MGEKF algorithm was further improved by P.J. Galkowski and M.A. Eslam [5]. In this paper, this improved MGEKF algorithm is explored for underwater applications with some modifications. In underwater, the noise in the measurements is very high, turning rate of the platforms is low and speed of the platforms is also low when compared with the missiles in air. These characteristics of the platform are studied in detail and the algorithm is modified suitably for tracking applications in underwater.

2 deals with mathematical modelling of bearing and elevation measurements. Section 3 describes the implementation of the filter and section 4 is about the results obtained in simulation.

Mathematical Modeling

Let a target be at a point P and the observer be at the origin, as shown in Fig-1. The measurement vector

$$Z, \text{ is written as } Z = \begin{bmatrix} B_m \\ \phi_m \end{bmatrix} = \begin{bmatrix} \tan^{-1} \frac{r_x}{r_y} + \sigma_B \\ r_z \\ \tan^{-1} \frac{r_{xy}}{r_z} + \sigma_\phi \end{bmatrix}$$

(1)

Where σ_B and σ_ϕ are zero mean, uncorrelated normally distributed errors in the bearing (B_m) and elevation (ϕ_m) measurements respectively.

Let the state vector be

$$X_s = \begin{bmatrix} \dot{x} & \dot{y} & \dot{z} & r_x & r_y & r_z \end{bmatrix}^T \quad (2)$$

The measurement matrix H is given by

$$H = \begin{bmatrix} 0 & 0 & 0 & \frac{\cos \hat{B}}{\hat{r}_{xy}} & -\frac{\sin \hat{B}}{\hat{r}_{xy}} & 0 \\ 0 & 0 & 0 & \frac{\cos \hat{\phi} \sin \hat{B}}{\hat{r}} & \frac{\cos \hat{\phi} \cos \hat{B}}{\hat{r}} & -\frac{\sin \hat{\phi}}{\hat{r}} \end{bmatrix} \quad (3)$$

Horizontal Plane And Bearing Measurements :-

If the range in horizontal plane is $\sqrt{r_x^2 + r_y^2}$,

then the estimated range be $\hat{r}_{xy} = \sqrt{r_x^2 + r_y^2}$ (4)

By adding r_{xy} and \hat{r}_{xy} , eqn. (5) is obtained .

$$r_{xy} + \hat{r}_{xy} = r_x \sin B + r_y \cos B + \hat{r}_x \sin \hat{B} + \hat{r}_y \cos \hat{B} \quad (5)$$

adding both sides $-r_x \sin \hat{B} - \hat{r}_x \sin \hat{B} - \hat{r}_y \cos B + r_y \cos \hat{B}$ to the above equation and after straight forward simplification, the following equations are obtained.

$$r_{xy} + \hat{r}_{xy} = \frac{(r_x - \hat{r}_x)(\sin B - \sin \hat{B}) + (r_y - \hat{r}_y)(\cos B - \cos \hat{B})}{1 - \cos(B - \hat{B})} \quad (6)$$

$$r_{xy} - \hat{r}_{xy} = \frac{(r_x - \hat{r}_x)(\sin B + \sin \hat{B}) + (r_y - \hat{r}_y)(\cos B + \cos \hat{B})}{1 + \cos(B - \hat{B})} \quad (7)$$

using (6) and (7)

$$2\hat{r}_{xy} = (r_x - \hat{r}_x) \left[\frac{\sin B - \sin \hat{B}}{1 - \cos(B - \hat{B})} - \frac{\sin B + \sin \hat{B}}{1 + \cos(B - \hat{B})} \right] + (r_y - \hat{r}_y) \left[\frac{\cos B - \cos \hat{B}}{1 - \cos(B - \hat{B})} + \frac{\cos B + \cos \hat{B}}{1 + \cos(B - \hat{B})} \right] \quad (8)$$

Eqn.(8) can be simplified as

$$\frac{\sin B - \sin \hat{B}}{1 - \cos(B - \hat{B})} - \frac{\sin B + \sin \hat{B}}{1 + \cos(B - \hat{B})} = \frac{(1 + \cos(B - \hat{B}))(\sin B - \sin \hat{B}) - (1 - \cos(B - \hat{B}))(\sin B + \sin \hat{B})}{1 - \cos^2(B - \hat{B})}$$

the coefficients of $(r_x - \hat{r}_x)$ and $(r_y - \hat{r}_y)$ are simplified and the above equation is rewritten as

$$2\hat{r}_{xy} = \frac{2\cos B(r_x - \hat{r}_x)}{\sin(B - \hat{B})} - \frac{2\sin B(r_y - \hat{r}_y)}{\sin(B - \hat{B})} \quad (9)$$

Again eqn. (9) is rewritten as

$$\sin(B - \hat{B}) = \frac{\cos B(r_x - \hat{r}_x) - \sin B(r_y - \hat{r}_y)}{\hat{r}_{xy}} \quad (10)$$

Elevation angle measurement:

In the previous section , it is seen that

$\tan^{-1} \frac{r_x}{r_y} = B$ generates

$$\sin(B - \hat{B}) = \frac{\cos B(r_x - \hat{r}_x) - \sin B(r_y - \hat{r}_y)}{\hat{r}_{xy}} \quad (11)$$

Similarly $\tan^{-1} \frac{r_{xy}}{r_z} = \phi$ generates

$$\sin(\phi - \hat{\phi}) = \frac{\cos \phi(r_{xy} - \hat{r}_{xy}) - \sin \phi(r_z - \hat{r}_z)}{r} \quad (12)$$

After simple trigonometric manipulations, eqn. (9) is written as

$$r_{xy} - \hat{r}_{xy} = \frac{(r_x - \hat{r}_x) \sin \frac{(B + \hat{B})}{2} + (r_y - \hat{r}_y) \cos \frac{(B + \hat{B})}{2}}{\cos \frac{(B - \hat{B})}{2}} \quad (13)$$

Substituting (13) in (12)

$$\sin(\phi - \hat{\phi}) = \frac{\cos \phi}{\hat{r}} \left[\frac{(r_x - \hat{r}_x) \sin \frac{(B + \hat{B})}{2} + (r_y - \hat{r}_y) \cos \frac{(B + \hat{B})}{2}}{\cos \frac{(B - \hat{B})}{2}} \right] -$$

$$\frac{\sin \phi}{\hat{r}} (r_z - \hat{r}_z) \quad (14)$$

Eqn. (10) and eqn.(14) are rewritten in matrix form as

$$\begin{bmatrix} (B - \hat{B}) \\ (\phi - \hat{\phi}) \end{bmatrix} = \begin{bmatrix} \frac{\cos B}{\hat{r}_{xy}} & -\frac{\sin B}{\hat{r}_{xy}} & 0 \\ \frac{\sin \left(\frac{B + \hat{B}}{2} \right) \cos \phi}{\cos \left(\frac{B - \hat{B}}{2} \right) \hat{r}} & \frac{\cos \left(\frac{B + \hat{B}}{2} \right) \cos \phi}{\cos \left(\frac{B - \hat{B}}{2} \right) \hat{r}} & -\frac{\sin \phi}{\hat{r}} \end{bmatrix}$$

$$\begin{bmatrix} r_x - \hat{r}_x \\ r_y - \hat{r}_y \\ r_z - \hat{r}_z \end{bmatrix} \quad (15)$$

As true bearing is not available, it is replaced by measured bearing in eqn.(15) and obtained eqn.(16) as follows.

$$\begin{bmatrix} (B - \hat{B}) \\ (\phi - \hat{\phi}) \end{bmatrix} = \begin{bmatrix} \frac{\cos B_m}{\hat{r}_{xy}} & -\frac{\sin B_m}{\hat{r}_{xy}} & 0 \\ \sin\left(\frac{B_m + \hat{B}}{2}\right)\cos\phi & \cos\left(\frac{B_m + \hat{B}}{2}\right)\cos\phi & -\sin\phi \\ \cos\left(\frac{B_m - \hat{B}}{2}\right)\hat{r} & \cos\left(\frac{B_m - \hat{B}}{2}\right)\hat{r} & \hat{r} \end{bmatrix} \begin{bmatrix} r_x - \hat{r}_x \\ r_y - \hat{r}_y \\ r_z - \hat{r}_z \end{bmatrix} = g \begin{bmatrix} r_x - \hat{r}_x \\ r_y - \hat{r}_y \\ r_z - \hat{r}_z \end{bmatrix} \quad (16)$$

Considering \dot{x} , \dot{y} and \dot{z} also, g is given by

$$g = \begin{bmatrix} 0 & 0 & 0 & \frac{\cos B_m}{\hat{r}_{xy} = \hat{r}_s \sin \hat{\phi}_m} & \frac{-\sin B_m}{\hat{r}_{xy} = \hat{r}_s \sin \hat{\phi}_m} & 0 \\ 0 & 0 & 0 & \cos\phi \sin\left(\frac{B_m + \hat{B}}{2}\right) & \cos\phi \cos\left(\frac{B_m + \hat{B}}{2}\right) & -\sin\phi \\ 0 & 0 & 0 & \hat{r} \cos\left(\frac{B_m - \hat{B}}{2}\right) & \hat{r} \cos\left(\frac{B_m - \hat{B}}{2}\right) & \hat{r} \end{bmatrix}$$

Implementation Of The Algorithm

The above mentioned improved algorithm is implemented using MGEKF (MGEKF equations are not given in this paper due to space constraint. These equations are available in [5].)for underwater passive target tracking as follows. As only bearing and elevation measurements are available, the velocity components of the target are assumed to be each 10 m/sec which is very close to the realistic speed of the vehicles in underwater. The range of the day, say 15000 meters, is utilized in the calculation of initial position estimate of the target is as $X(0|0)=[10 \ 10 \ 10 \ 15000\sin B_m(0)\sin \phi_m(0) \ 15000\sin \phi_m(0)\cos B_m(0) \ 15000\cos \phi_m(0)]^T$ where $B_m(0)$ and $\phi_m(0)$ are initial bearing and elevation measurements.

Simulation Results

All raw bearings and elevation measurements are corrupted by additive zero mean Gaussian noise with a r.m.s level of 0.3 degree. Corresponding to a tactical scenario in which the target is at the initial range of 20000 meters at initial bearing and elevation of 0 and 45 degrees respectively. The target is assumed to be moving at a constant course of 140 degrees. Observer is moving

in a straight line with course of 90 degrees. The results have been ensemble averaged over several Monte Carlo runs. The errors in estimates are plotted in Fig.2. It is observed that this required accuracy is obtained from 400 seconds onwards and so this algorithm seems to be very much useful for underwater passive target tracking when observer is moving, for a moving target.

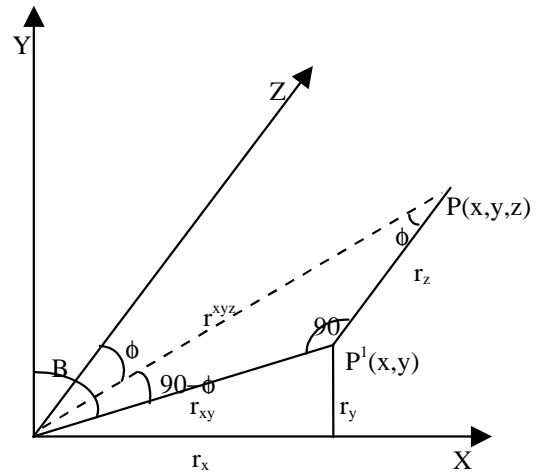


Fig.1. A typical target observer geometry

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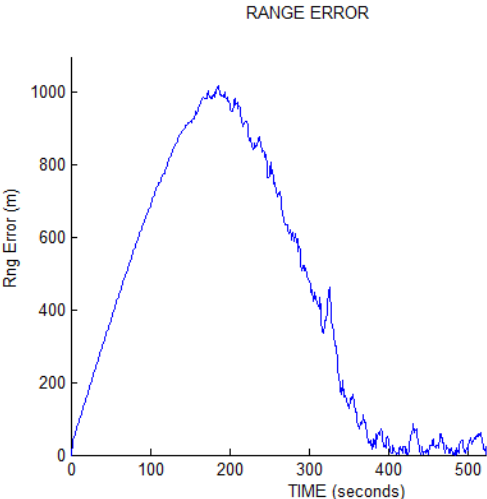


Fig.2(a). Error in range estimate versus time

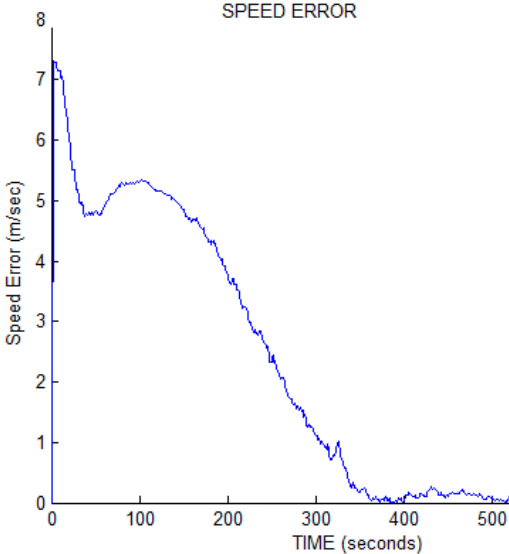


Fig.2(b). Error in Speed estimate versus time

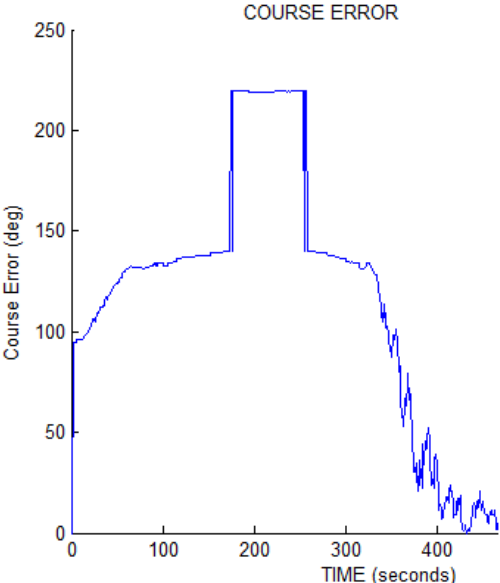


Fig.2(c). Error in Course estimate verses time